## Week 2: Data Summary and Visualization

## 1. Categorical variables I

Stat 140 - 04

Mount Holyoke College

#### 1. Questions? 15 min

2. Today: Categorical variables

#### 3. Main ideas

- 1. Distributions
- 2. Proportional reasoning
- Contingency table

## 4. Summary

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The categorical variables identify a category for each case. They have a limited number of different values, called **levels**.

## Examples:

If our observational units are 100 M&M's. Color of a M&M is a categorical variable.

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Distribution is about "pattern of variation in a variable"

The key of distribution is to focus on the variation across the entire data set.



individual level color of the MM is blue



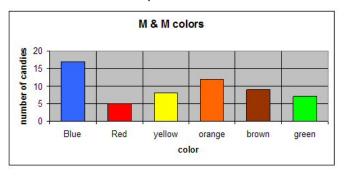
macro level colors of all MM's

In this class, we focus on distribution of categorical variable.

For a categorical variable, the distribution

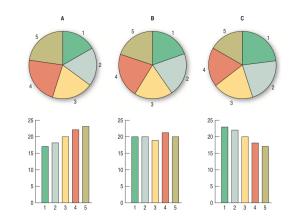
- ▶ names the possible levels in a categorical variable
- ▶ tells how many times each occurs

We can visualize the distribution by a bar plot or a pie char. In this course, we focus on bar plot.



#### Pie chart is not good for visualizing the relative frequencies

Three pie charts that look pretty much alike along with bar charts of the same data. The bar charts show three distinctly different patterns, but it is almost impossible to see those in the pie charts.



Suppose we have a data set that consists of almost 54,000 diamonds that contains the prices and their attributes (e.g cut, color, clarity).

#### Poll question

Which command would help you take a glimpse of the data?

- 1. ncol(diamonds)
- 2. nrow(diamonds)
- 3. glimpse(diamonds)

## The data table is given as follow

| carat<br><dbl></dbl> | cut<br><ord></ord> | color<br><ord></ord> | <b>clarity</b><br><ord></ord> | depth<br><dbl></dbl> | table<br><dbl></dbl> | price <int></int> |
|----------------------|--------------------|----------------------|-------------------------------|----------------------|----------------------|-------------------|
| 0.23                 | Ideal              | E                    | SI2                           | 61.5                 | 55                   | 326               |
| 0.21                 | Premium            | E                    | SI1                           | 59.8                 | 61                   | 326               |
| 0.23                 | Good               | E                    | VS1                           | 56.9                 | 65                   | 327               |
| 0.29                 | Premium            | 1                    | VS2                           | 62.4                 | 58                   | 334               |
| 0.31                 | Good               | J                    | SI2                           | 63.3                 | 58                   | 335               |
| 0.24                 | Very Good          | J                    | VVS2                          | 62.8                 | 57                   | 336               |

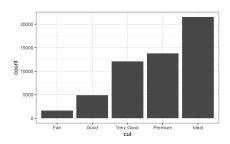
6 rows | 1-7 of 10 columns

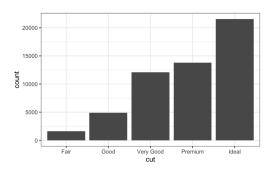
When a variable is categorical, you can visualize the distribution with a bar plot. There are lots of ways to make bar plots in R. Throughout this course, we will use the package 'ggplot2' to make our visualizations.

For example, the code below plots a bar plot of the 'cut' variable.

#### Rcode

```
ggplot(data = diamonds) +
  geom_bar(mapping = aes(x = cut))
```



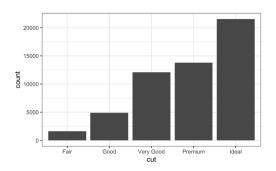


#### Poll question

What does the y axis represent in the bar plot?

- 1. Count of diamond in each category
- 2. Frequencies of diamond in each category
- 3. The total number of diamonds

## Example: Diamond!



#### Poll question

How many diamonds in the dataset had a 'Good' cut?

- 1. 2000
- 2. 5000
- 3. 7000

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The bar plot displays the counts – how many times each value appears in the data – on the y-axis. You can also organize this information in a **frequency table**. Note the term frequency refers to the number of times each value occurs in the respective data set.

| cut     n <ord><int>       Fair     1610       Good     4906       Very Good     12082       Premium     13791       Ideal     21551</int></ord> |           |       |  |
|--|-----------|-------|--|
| Good 4906 Very Good 12082 Premium 13791  |           |       |  |
| Very Good 12082<br>Premium 13791   | Fair      | 1610  |  |
| Premium 13791  | Good      | 4906  |  |
|  | Very Good | 12082 |  |
| ldeal 21551  | Premium   | 13791 |  |
|  | Ideal     | 21551 |  |

Using the frequency table, one can calculate a notion of proportion.

For example, in the diamond dataset, if we know there are 53,940 units in the sample, and we know 21,551 of them have 'ideal' cut. Calculate the proportion of diamonds that have 'Ideal' cut.

$$\frac{21,551}{53,940} = 0.3995 = 40\%$$

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If we are interested in knowing the relationship between categorical variables, we can look at the contingency table.

| color<br><ord></ord> | Fair<br><int></int> | Good<br><int></int> | Very Good<br><int></int> | Premium <int></int> | Ideal<br><int></int> |
|----------------------|---------------------|---------------------|--------------------------|---------------------|----------------------|
| D                    | 163                 | 662                 | 1513                     | 1603                | 2834                 |
| Е                    | 224                 | 933                 | 2400                     | 2337                | 3903                 |
| F                    | 312                 | 909                 | 2164                     | 2331                | 3826                 |
| G                    | 314                 | 871                 | 2299                     | 2924                | 4884                 |
| Н                    | 303                 | 702                 | 1824                     | 2360                | 3115                 |
| 1                    | 175                 | 522                 | 1204                     | 1428                | 2093                 |
| J                    | 119                 | 307                 | 678                      | 808                 | 896                  |

The entries in the table count how many observational units are in each combination of levels of the cut and color variables. If you add up all the numbers in the table, you will get the total number of observational units in the sample.

## Calculate the proportion of diamonds that have 'cut' Fair and 'color' E

| color<br><ord></ord> | Fair <int></int> | Good<br><int></int> | Very Good<br><int></int> | Premium <int></int> | Ideal<br><int></int> |
|----------------------|------------------|---------------------|--------------------------|---------------------|----------------------|
| D                    | 163              | 662                 | 1513                     | 1603                | 2834                 |
| Е                    | 224              | 933                 | 2400                     | 2337                | 3903                 |
| F                    | 312              | 909                 | 2164                     | 2331                | 3826                 |
| G                    | 314              | 871                 | 2299                     | 2924                | 4884                 |
| Н                    | 303              | 702                 | 1824                     | 2360                | 3115                 |
| 1                    | 175              | 522                 | 1204                     | 1428                | 2093                 |
| J                    | 119              | 307                 | 678                      | 808                 | 896                  |

# Calculate the proportion of diamonds fall in 'cut' Fair (aggregating across all values of 'color')

| color<br><ord></ord> | Fair <int></int> | Good<br><int></int> | Very Good<br><int></int> | Premium<br><int></int> | <b>Ideal</b> <int></int> |
|----------------------|------------------|---------------------|--------------------------|------------------------|--------------------------|
| D                    | 163              | 662                 | 1513                     | 1603                   | 2834                     |
| E                    | 224              | 933                 | 2400                     | 2337                   | 3903                     |
| F                    | 312              | 909                 | 2164                     | 2331                   | 3826                     |
| G                    | 314              | 871                 | 2299                     | 2924                   | 4884                     |
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Among those cases where the diamonds have 'cut' Fair , calculate the proportion of diamonds that have 'color' E.

| color<br><ord></ord> | Fair<br><int></int> | Good<br><int></int> | Very Good<br><int></int> | Premium <int></int> | <b>Ideal</b> <int></int> |
|----------------------|---------------------|---------------------|--------------------------|---------------------|--------------------------|
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## Summary of main ideas

- 1. Distributions
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